

## Quadratic function

1. Given  $f(x) = x^2 + 6x + 10$ , find the factored form (if possible) and the vertex form of the function  $f$ . is the range and axis of symmetry of the graph  $y = f(x)$ .

Ans.  $f(x) = (x + 3)^2 + 1$ , no factored form,  $f(D) = [1; +\infty)$ ,  $x = -3$

2. For the function  $f(x) = 2x^2 + 4x + 5$  find:

- the coordinates of the vertex of the parabola.
- the vertex form of the function  $f$ .
- the range of the function  $f$ .
- the lowest value and intervals on which the function increases and decreases.

Ans. a)  $V(-1, 3)$ , b)  $f(x) = 2(x + 1)^2 + 3$  c)  $f(D) = [3; +\infty)$  d)  $y_{\min} = 3$   $V(-1, 3)$ ,  $f \uparrow: [-1; +\infty)$   $f \downarrow: (-\infty; -1]$

3. The point  $V(4, 0)$  is the vertex of the graph of the function  $f(x) = 2x^2 + bx + c$ . Find  $b, c$ .

Ans.  $f(x) = 2(x - 4)^2 = 2x^2 - 16x + 32$

4. The greatest value of the function  $f$  is equal to 4 for  $x = -3$ . The point  $P(-1, 3)$  lies on the graph of the function  $f$ . Find the formula of the function  $f$ .

Ans.  $f(x) = -0.25(x + 3)^2 + 4$

5. The quadratic function is given by the formula  $f(x) = ax^2 + bx + c$ . Find  $a, b, c$ , knowing that all positive values of the function  $f$  are in the interval  $(0, 12)$  and the greatest value of the function  $f$  is equal to 9.

Ans.  $a = -\frac{1}{4}$ ,  $b = 3$ ,  $c = 0$

6. The function  $f(x) = x^2 + bx + c$  satisfies the following condition.  
 $f(-1) = f(3) = 1$ . Find the value of the coefficient  $b$ .

Ans.  $b = -2$ ,

7. A function  $g$  is quadratic. The line  $x = 3$  is the axis of symmetry of the parabola  $y = g(x)$  and  $x_1 = 1$  is one of the zeros of the function  $g$ . The point  $P(2, -6)$  lies on the parabola. Write the factored form and the standard form of the function  $g$ .

Ans.  $g(x) = 2(x - 1)(x - 5)$

8. Write the general form of a quadratic function  $f$ , if the point  $V(-3, 4)$  is the vertex of the parabola  $y = f(x)$  and the point  $A(-6, -5)$  lies on the graph of function  $f$ .

Ans.  $f(x) = -x^2 - 6x - 5$

9. The graph of a function  $f$  passes through points  $(1, 1)$  and  $(-1, -1)$ . Prove that the function  $f$  has two zeros, product of which is equal to  $-1$ .

10. Given the function  $f(x) = x^2 - 6x$ , find the smallest integer value of  $c$ , such that the function  $k(x) = f(x) + c$  cannot be written in a factored form.

Ans.  $c = 10$

11. Find the general form of a quadratic function, if the graph of the function passes through points  $A(-2, -3)$ ,  $B(0, -3)$ ,  $C(2, 5)$

Ans.  $f(x) = x^2 + 2x - 3$