

## 1. Real Numbers with solutions

**Task 1.01.** (0-1) (2015 - task 07)

Let us assume that  $\frac{15}{16}$  is approximately equal to 0.9. The approximation error expressed as a percentage will be equal to

- A. 4%                      B. 0.04%                      C. 3%                      D. 0.03%

**Solution 1.01. A**

$$\frac{\left| \frac{15}{16} - 0.9 \right|}{\frac{15}{16}} \times 100\% = \left| \frac{15}{16} - \frac{9}{10} \right| \times \frac{16}{15} \times 100\% = \frac{6}{160} \times \frac{1600}{15} \% = 4\%$$

**Task 1.02.** (0-1) (2016 - task 01)

The following table shows the number of votes received by each candidate in a by-election.

Candidate	I	II
Number of votes	13970	17780

The number of votes received by the winner was higher than the number of votes received by the other candidate by:

- A. 56 percentage points.                      B. 44 percentage points.  
C. 27 percentage points.                      D. 12 percentage points.

**Solution 1.02. D**

Number of all votes:  $17780 + 13970 = 31750$ .

Winner percentage result:  $\frac{17780}{31750} \times 100\% = 56\%$ .

Other candidate percentage result: 44%.

A percentage point (pp) is the unit for the arithmetic difference of two percentages:  $56\% - 44\% = 12$  pp.

## 1. Real Numbers with solutions

**Task 1.03.** (0-1) (2016 - task 02)

If  $\log a = \frac{1}{2}$  and  $\log b = \frac{2}{5}$ , where  $a > 0$  and  $b > 0$ , then the value of the expression

$\log(a^2b)$  equals

- A.  $\frac{7}{5}$                       B.  $\frac{4}{10}$                       C.  $\frac{13}{20}$                       D.  $\frac{1}{10}$

**Solution 1.03. A**

$$\log(a^2b) = \log(a^2) + \log(b) = 2 \log(a) + \log(b) = 2 \times \frac{1}{2} + \frac{2}{5} = \frac{7}{5}$$

**Task 1.04.** (0-1) (2016 - task 03)

The number  $4(4^{18} + 4^{17})$  equals

- A.  $4^{35}$                       B.  $4^{36}$                       C.  $5 \times 4^{17}$                       D.  $5 \times 4^{18}$

**Solution 1.04. D**

$$4(4^{18} + 4^{17}) = 4 \times 4^{17}(4 + 1) = 4^{18} \times 5$$

**Task 1.05.** (0-1) (2017 - task 01)

It may be assumed that 0.3 is an approximation of  $\frac{5}{16}$ . What is the percentage error of this approximation?

- A. 2.5%                      B. 0.025%                      C. 4%                      D. 0.04%

**Solution 1.05. C**

$$\frac{\left| \frac{5}{16} - 0.3 \right|}{\frac{5}{16}} \times 100\% = \left| \frac{5}{16} - \frac{3}{10} \right| \times \frac{16}{5} \times 100\% = \frac{2}{160} \times \frac{1600}{5} \% = 4\%$$

**Task 1.06.** (0-1) (2017 - task 02)

Among those listed below, the only positive number is:

- A.  $(-3)^0$                       B.  $-3^0$                       C.  $(-3)^{2017}$                       D.  $-3^{2017}$

**Solution 1.06. A**

$$(-3)^0 = 1 > 0 \qquad -3^0 = -1 < 0 \qquad (-3)^{2017} = -3^{2017} < 0$$

## 1. Real Numbers with solutions

**Task 1.07.** (0-1) (2018 - task 10)

In February, the price of a certain product remained constant, but on March 1<sup>st</sup> it was increased by 10%. After a week, the new price was decreased by 20%. As a result of these two changes, the initial price of the product was decreased by

- A. 12%                      B. 14%                      C. 9%                      D. 4%

**Solution 1.07. A**

Let  $x$  be the first price.

The increase factor is  $100\% + 10\% = 110\% = 1.1$ .

The decrease factor is  $100\% - 20\% = 80\% = 0.8$ .

After the two price changes the new price will be 12% less

because:  $x \times 1.1 \times 0.8 = x \times 0.88 = 88\%x = x - 12\%x$

**Task 1.08.** (0-1) (2019 - task 01)

If we assume that  $\frac{8}{9}$  is approximately equal to 0.9/ the percentage error of this approximation is equal to:

- A. 1%                      B. 1.25%                      C. 0.0125%                      D. 0.01%

**Solution 1.08. B**

$$\frac{\left| \frac{8}{9} - 0.9 \right|}{\frac{8}{9}} \times 100\% = \left| \frac{8}{9} - \frac{9}{10} \right| \times \frac{9}{8} \times 100\% = \frac{1}{90} \times \frac{900}{8} \% = 1.25\%$$

## 1. Real Numbers with solutions

**Task 1.09.** (0-1) (2020 - task 01)

The reciprocal of  $3\frac{2}{9} - 5\frac{1}{3} \times \sqrt{\frac{49}{144}}$  is:

- A.  $-9$                       B.  $-\frac{1}{9}$                       C.  $\frac{1}{9}$                       D.  $9$

**Solution 1.09. C**

$$3\frac{2}{9} - 5\frac{1}{3} \times \sqrt{\frac{49}{144}} = 3\frac{2}{9} - \frac{16}{3} \times \frac{7}{12} = \frac{29}{9} - \frac{28}{9} = \frac{1}{9}$$

**Task 1.10.** (0-1) (2020 - task 05)

The number  $\frac{4^8+4^7}{320 \times 4^4}$  is equal to:

- A.  $4^{-1}$                       B.  $4^0$                       C.  $4^1$                       D.  $4^2$

**Solution 1.10. B**

$$\frac{4^8 + 4^7}{320 \times 4^4} = \frac{4^7(4 + 1)}{4^3 \times 5 \times 4^4} = 1 = 4^0$$

**Task 1.11.** (0-1) (2020 - task 06)

If  $\log_3 5 = 0.68$  then  $\log_3 45$  equals:

- A.  $1.32$                       B.  $1.36$                       C.  $2.68$                       D.  $6.8$

**Solution 1.11. C**

$$\log_3 45 = \log_3(3^2 \times 5) = \log_3(3^2) + \log_3(5) \approx 2 + 0.68 = 2.68$$

## 1. Real Numbers with solutions

**Task 1.12.** (0-1) (2021 - task 02)

The Seine is shorter than the Vistula by 25%, and the Rhine is longer than the Vistula by 17%. Thus the Rhine is longer than the Seine by

- A. 64%                      B. 56%                      C. 42%                      D. 21%

**Solution 1.12. B**

Let  $S$  be the length of Seine river.

Let  $V$  be the length of Vistula river.

Let  $R$  be the length of Rhine river.

$$S = 0.75V \quad R = 1.17V$$

$$\frac{R-S}{S} = \frac{1.17V-0.75V}{0.75V} = \frac{0.42V}{0.75V} = \frac{42}{75} = \frac{14}{25} = \frac{56}{100} = 56\%$$

**Task 1.13.** (0-4) (2021- task 18)

Write down each of the sentences a–d below as an algebraic expression.

- a) The difference of  $a$  squared and  $b$ .

.....

- b) The absolute value of the sum of  $b$  and tripled  $a$ .

.....

- c) The quotient of  $a$  squared and the third power of  $b$ .

.....

- d) The product of  $a$  increased by 5 and the square root of  $b$ .

.....

**Solution 1.13.**

1.13 a)  $a^2 - b$

b)  $|b + 3a|$

c)  $a^2 \div b^3$

d)  $(a + 5) \times \sqrt{b}$

## 1. Real Numbers with solutions

### Answers

1.01 A	1.02 D	1.03 A	1.04 D	1.05 C
1.06 A	1.07 A	1.08 B	1.09 C	1.10 B
1.11 C	1.12 B			

1.13 a)  $a^2 - b$

b)  $|b + 3a|$

c)  $a^2 \div b^3$

d)  $(a + 5) \times \sqrt{b}$